

# A value-of-information approach to sample size determination and decision-making in confirmatory clinical trials in small populations

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# Levels of evidence requirements in rare diseases

Regulation (EC) 141/2000:

*“patients with [rare] conditions deserve the same quality, safety and efficacy in medicinal products as other patients”*

*“orphan products should therefore be submitted to the normal evaluation process”*

FDA Draft Guidance on Rare Diseases:

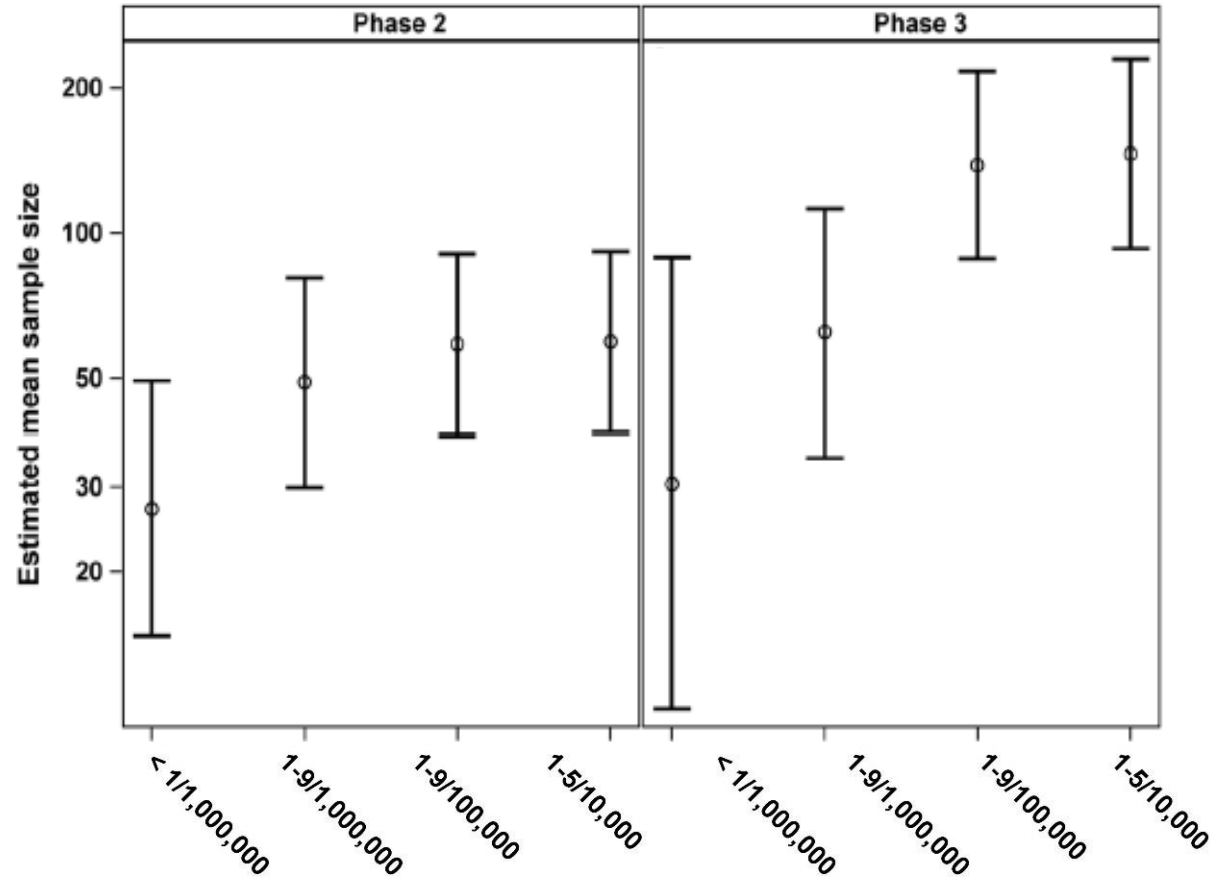
*“The Orphan Drug Act [...] does not create a statutory standard [...] different from [...] common conditions”*



## Sample sizes for rare disease trials from clinicaltrials.gov database

Sample size	Non-rare disease	Rare disease
500+	8%	1%
101 – 500	30%	13%
51 – 100	22%	19%
0 – 50	40%	67%

For rare diseases grouped by prevalence...



## Example of a trial in haemophilia A

E: tailored prophylaxis with recombinant factor VIII

C: usual care

Expected prob. of success on C,  $p_C = 0.55$

Expected prob. of success on E,  $p_E = 0.79$

Conventional sample size calculation:

type I error rate,  $\alpha = 0.05$  (two-sided)

power,  $1 - \beta = 0.9$

total sample size,  $n = 150$  (75 per arm)

Rare disease: size of total population to be treated = 4000

600 on C	3250	
75 on C	75 on E	

Trial cost: \$1,000,000 + \$5,000 per patient

Additional cost for E: \$61,000 per patient

Treatment success value: \$400,000 per patient

E(gain) relative to all receiving C: if  $p_C = p_E = 0.55$

-\$1,000,000 - \$5,000 × 150      -\$61,000 × 3250 × 0.025

-\$61,000 × 75

= -\$11 million



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-\$1,000,000 - \$5,000 × 150

-\$61,000 × 75

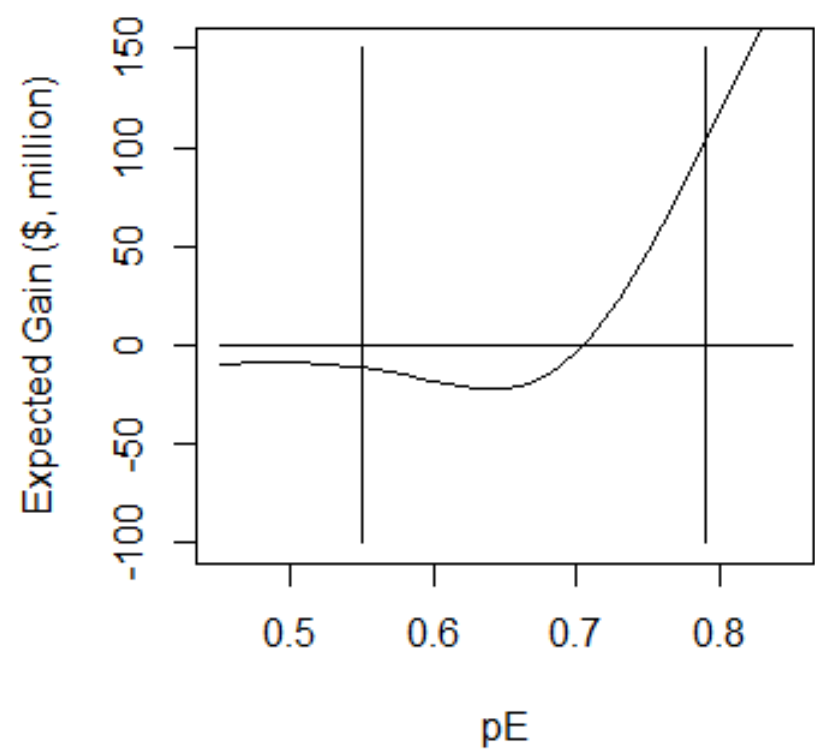
+\$400,000 × 75 × 0.24

-\$61,000 × 3250 × 0.9

+\$400,000 × 3250 × 0.9 × 0.24

= \$103 million







Impact of reducing to 80% power:

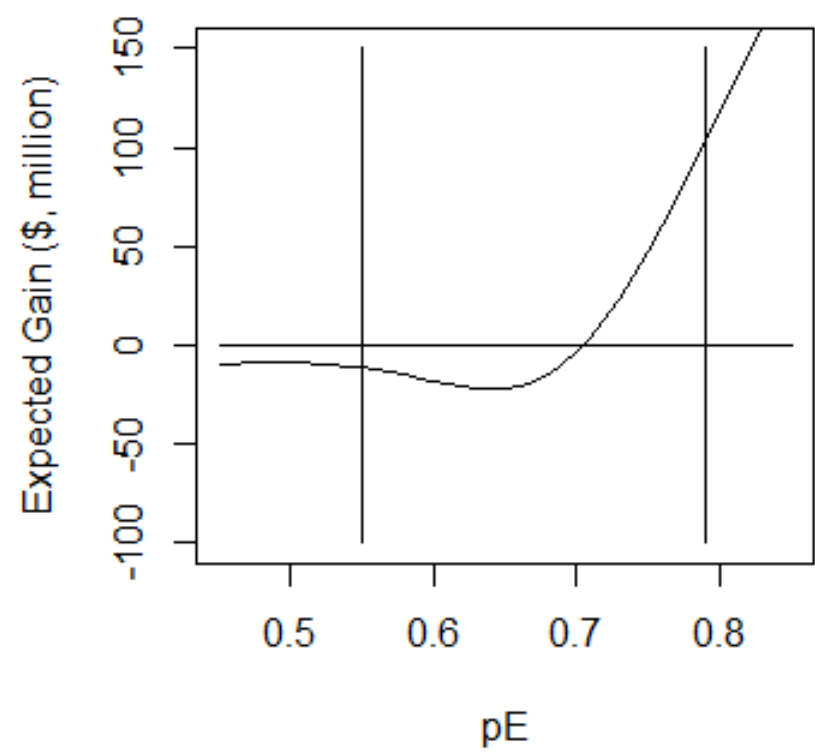
448 on C		3440
56 on C	56 on E	

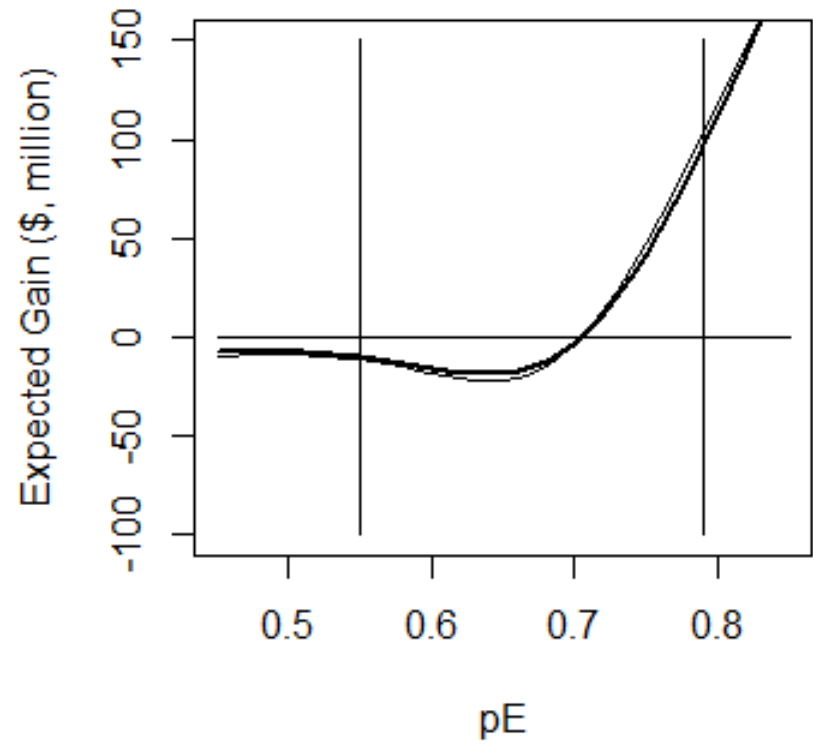
E(gain) relative to all receiving C: if  $p_C = p_E = 0.55$

$$\begin{aligned}
 &-\$1,000,000 - \$5,000 \times 112 && -\$61,000 \times 3440 \times 0.025 \\
 &-\$61,000 \times 56
 \end{aligned}$$

E(gain) relative to all receiving C: if  $p_C = 0.55, p_E = 0.79$

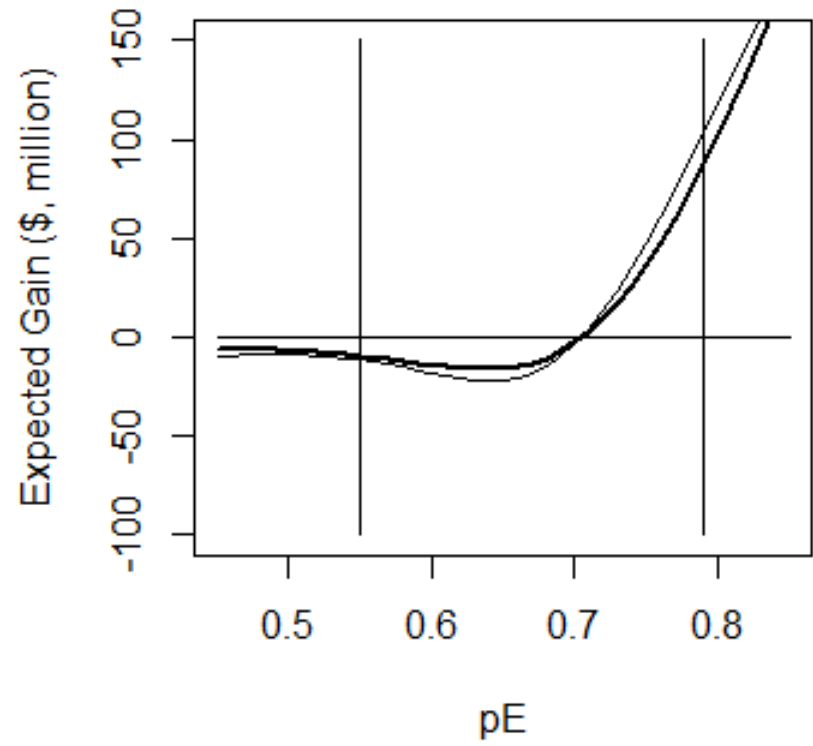
$$\begin{aligned}
 &-\$1,000,000 - \$5,000 \times 112 && -\$61,000 \times 3440 \times 0.8 \\
 &-\$61,000 \times 56 && +\$400,000 \times 3440 \times 0.8 \times 0.24 \\
 &+\$400,000 \times 56 \times 0.24
 \end{aligned}$$





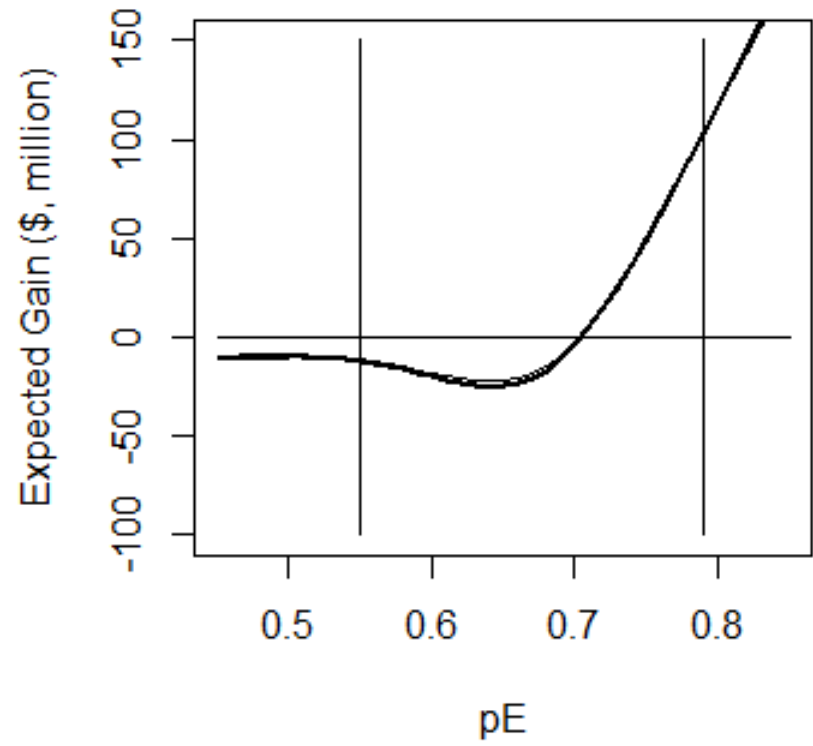
power = 0.8





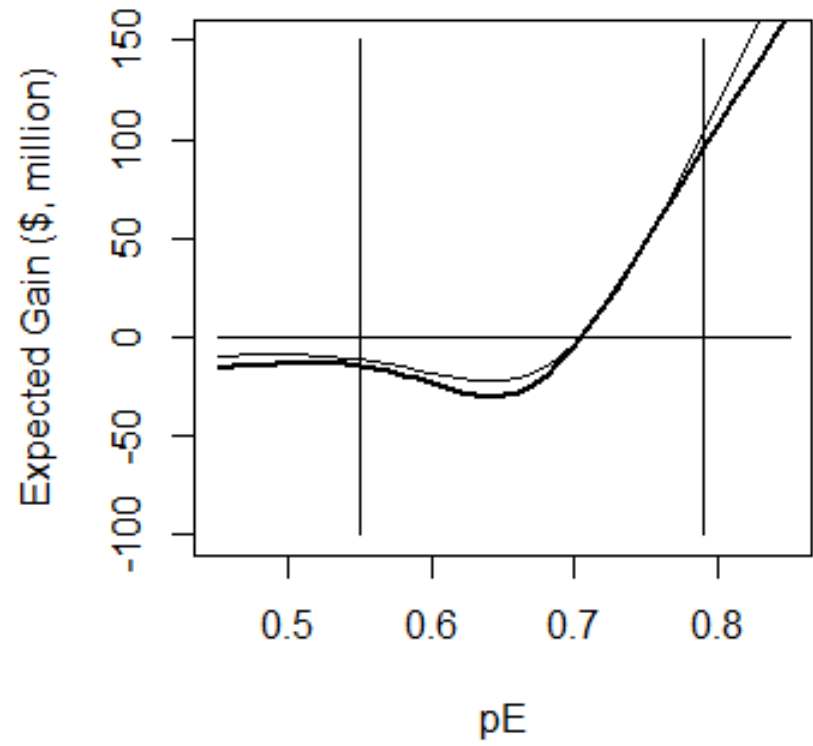
power = 0.7





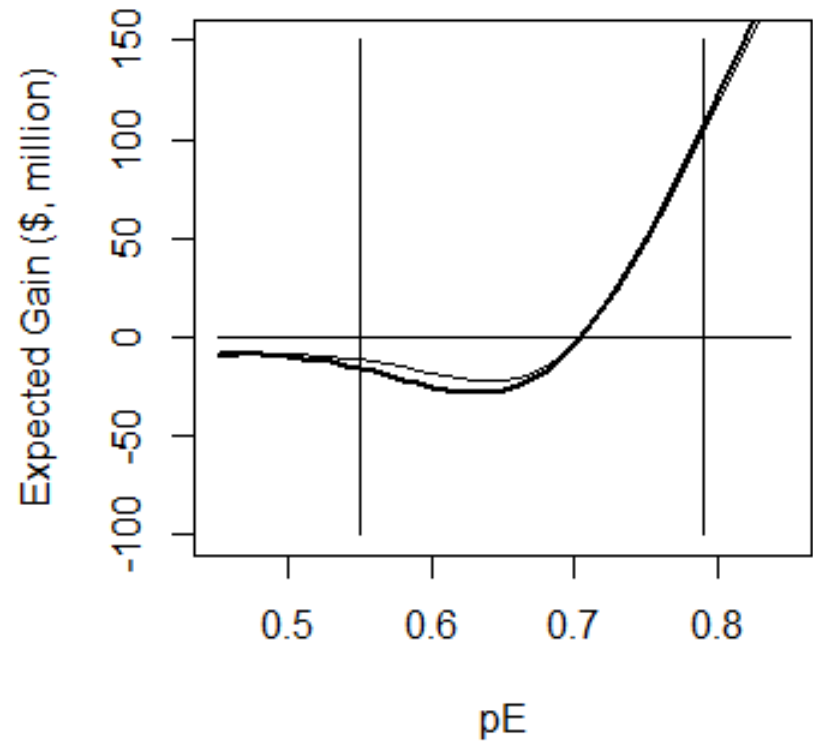
power = 0.95





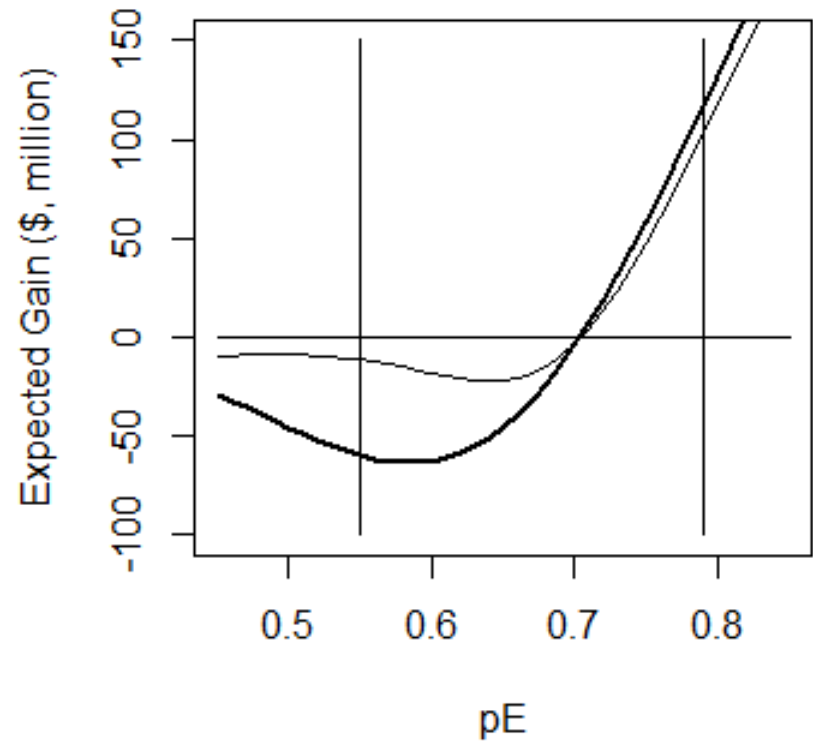
power = 0.99





$$\alpha = 0.1$$



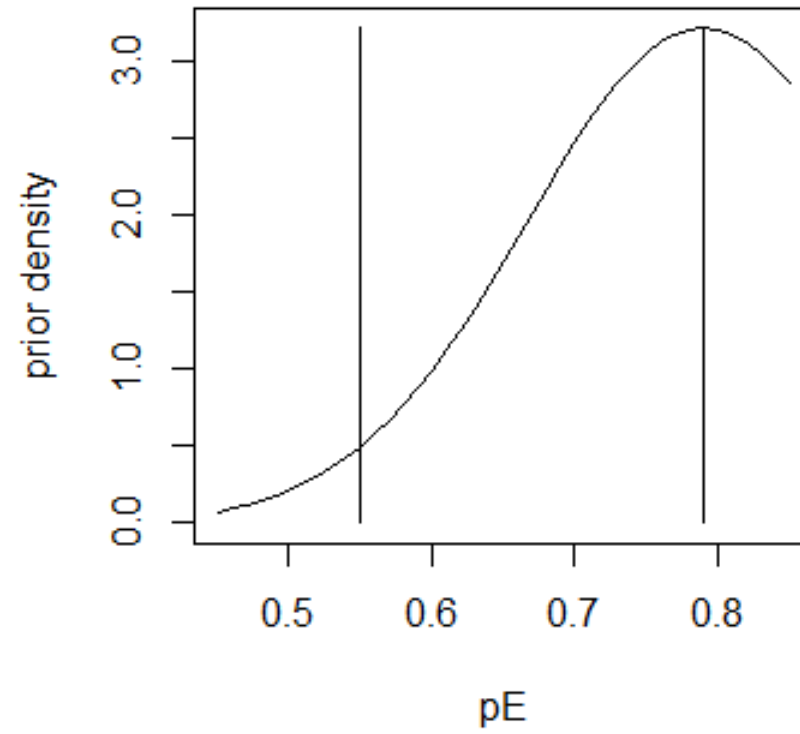


$$\alpha = 0.5$$

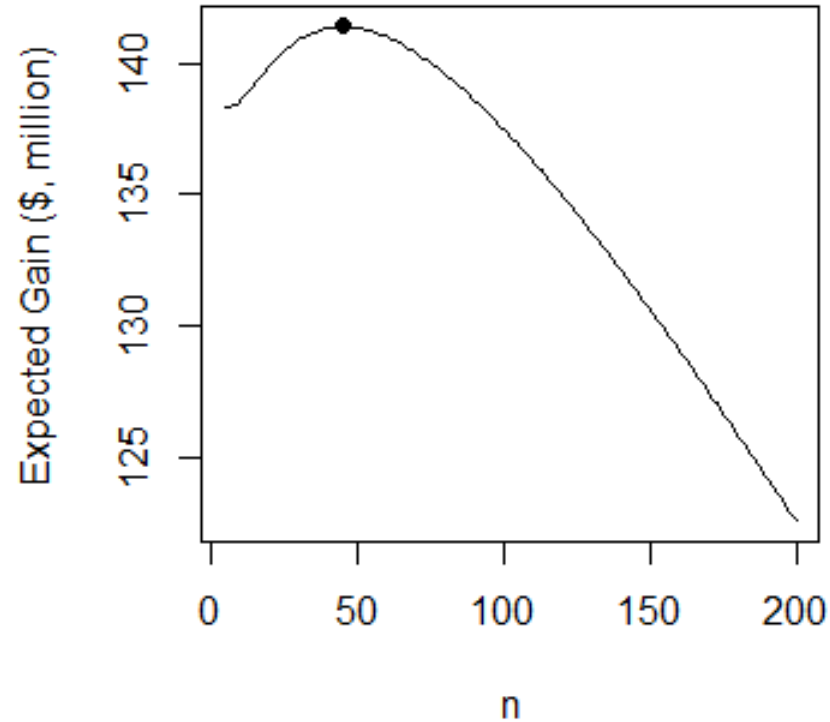




# Prior distribution



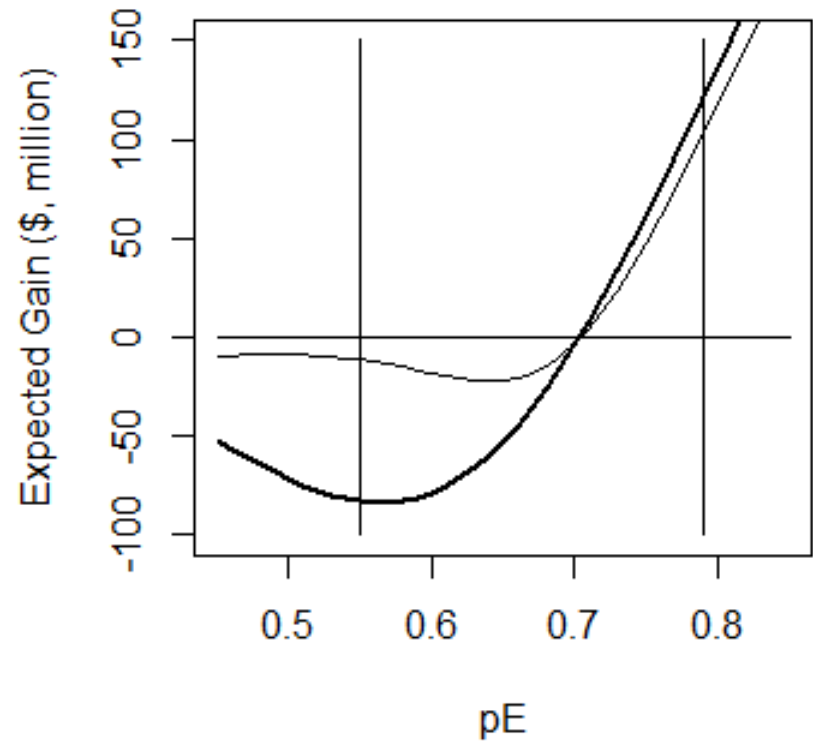
Design optimization: E(gain) for optimal  $\alpha$  for range of  $n$



Optimal design has  $n = 46$  (23 per arm)

$$\alpha = 0.35$$

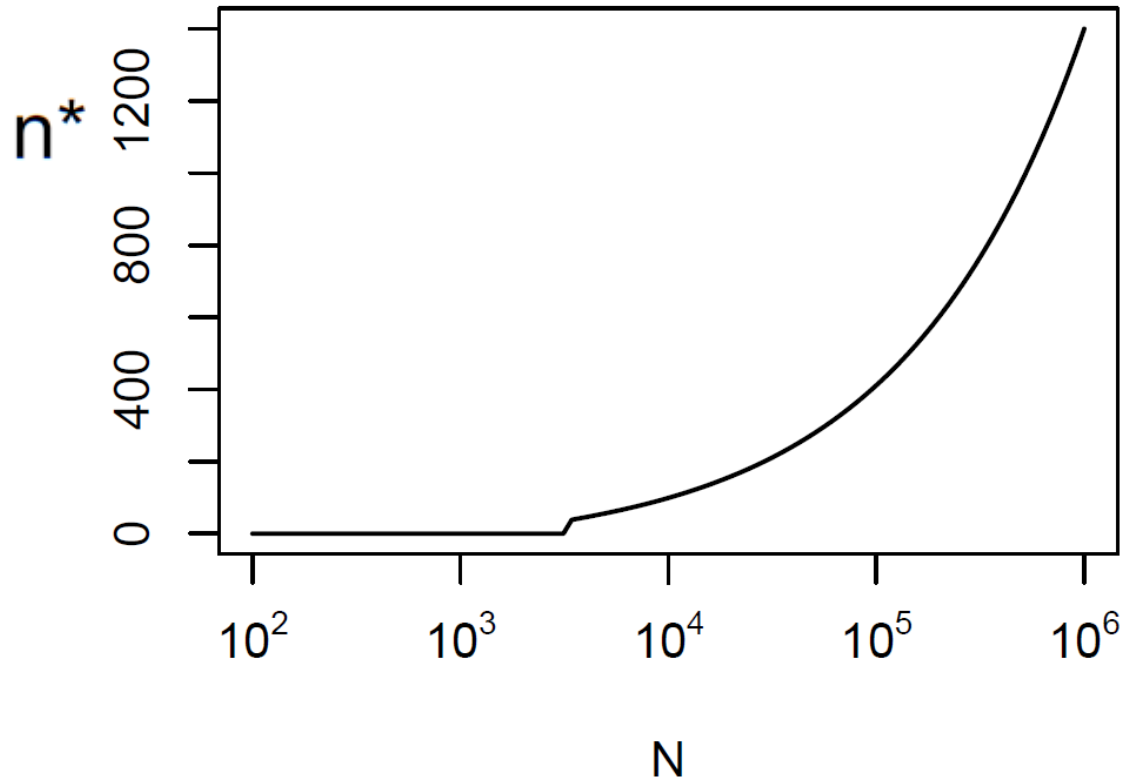




$$\alpha = 0.35, n = 46$$



## Effect of population size – (i) on optimal trial sample size

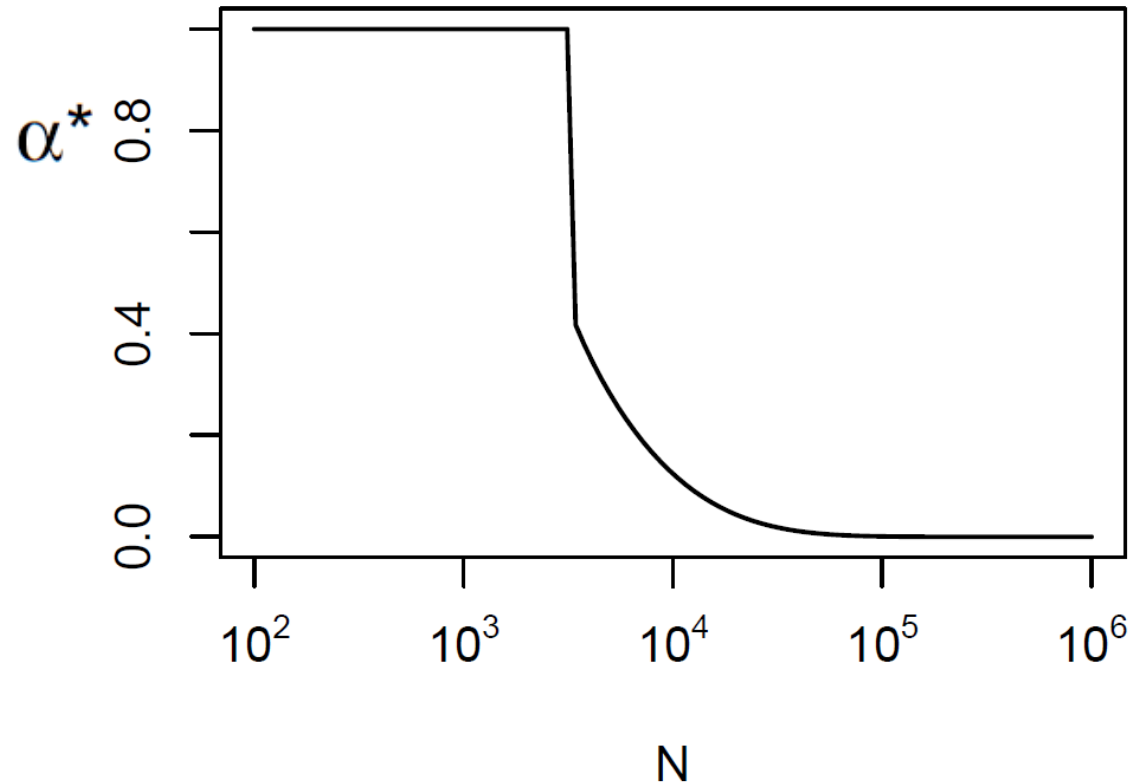


Optimal sample size smaller for smaller population size  $N$ :

$$n \propto N^{1/2} \text{ for large } N$$

For small  $N$  optimal to approve new treatment without a trial!

## Effect of population size– (ii) on optimal significance level



Optimal  $\alpha$  larger for smaller population size:

small  $N$ :  $\alpha > 0.05$

large  $N$ :  $\alpha < 0.05$

Decision reflects population size

## Summary

Trials in rare diseases do currently use smaller sample sizes

Value-of-information methods

- could formalise ad-hoc sample size choice

- modify sample size according to population size by considering value of information gained

- lead to clinical decision-making reflecting gain to population

- do not increase information available from small trial

Not the last word; but maybe part of a conversation

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